## GCE Examinations

## Advanced Subsidiary

## Core Mathematics C1

Paper D<br>Time: 1 hour 30 minutes

## Instructions and Information

Candidates may NOT use a calculator in this paper
Full marks may be obtained for answers to ALL questions.
Mathematical formulae and statistical tables are available.
This paper has ten questions.

## Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.

1. Express $\sqrt{50}+3 \sqrt{8}$ in the form $k \sqrt{2}$.
2. Differentiate with respect to $x$

$$
\begin{equation*}
3 x^{2}-\sqrt{x}+\frac{1}{2 x} \tag{4}
\end{equation*}
$$

3. A sequence is defined by the recurrence relation

$$
\begin{equation*}
u_{n+1}=u_{n}-2, \quad n>0, \quad u_{1}=50 . \tag{1}
\end{equation*}
$$

(a) Write down the first four terms of the sequence.
(b) Evaluate

$$
\begin{equation*}
\sum_{r=1}^{20} u_{r} \tag{3}
\end{equation*}
$$

4. (a) Find the value of the constant $k$ such that the equation

$$
\begin{equation*}
x^{2}-6 x+k=0 \tag{2}
\end{equation*}
$$

has equal roots.
(b) Solve the inequality

$$
\begin{equation*}
2 x^{2}-9 x+4<0 . \tag{4}
\end{equation*}
$$

5. Solve the simultaneous equations

$$
\begin{align*}
& x+y=2 \\
& 3 x^{2}-2 x+y^{2}=2 \tag{7}
\end{align*}
$$

6. Given that

$$
\frac{\mathrm{d} y}{\mathrm{~d} x}=3 \sqrt{x}-x^{2},
$$

and that $y=\frac{2}{3}$ when $x=1$, find the value of $y$ when $x=4$.
7. The first three terms of an arithmetic series are $(12-p), 2 p$ and $(4 p-5)$ respectively, where $p$ is a constant.
(a) Find the value of $p$.
(b) Show that the sixth term of the series is 50 .
(c) Find the sum of the first 15 terms of the series.
(d) Find how many terms of the series have a value of less than 400 .
8.

$$
\begin{equation*}
\mathrm{f}(x)=2 x^{2}+3 x-2 \tag{2}
\end{equation*}
$$

(a) Solve the equation $\mathrm{f}(x)=0$.
(b) Sketch the curve with equation $y=\mathrm{f}(x)$, showing the coordinates of any points of intersection with the coordinate axes.
(c) Find the coordinates of the points where the curve with equation $y=\mathrm{f}\left(\frac{1}{2} x\right)$ crosses the coordinate axes.

When the graph of $y=\mathrm{f}(x)$ is translated by 1 unit in the positive $x$-direction it maps onto the graph with equation $y=a x^{2}+b x+c$, where $a, b$ and $c$ are constants.
(d) Find the values of $a, b$ and $c$.
9.


Figure 1
Figure 1 shows the curve $C$ with the equation $y=x^{3}+3 x^{2}-4 x$ and the straight line $l$.
The curve $C$ crosses the $x$-axis at the origin, $O$, and at the points $A$ and $B$.
(a) Find the coordinates of $A$ and $B$.

The line $l$ is the tangent to $C$ at $O$.
(b) Find an equation for $l$.
(4)
(c) Find the coordinates of the point where $l$ intersects $C$ again.
10. The straight line $l_{1}$ has equation $2 x+y-14=0$ and crosses the $x$-axis at the point $A$.
(a) Find the coordinates of $A$.

The straight line $l_{2}$ is parallel to $l_{1}$ and passes through the point $B(-6,6)$.
(b) Find an equation for $l_{2}$ in the form $y=m x+c$.

The line $l_{2}$ crosses the $x$-axis at the point $C$.
(c) Find the coordinates of $C$.

The point $D$ lies on $l_{1}$ and is such that $C D$ is perpendicular to $l_{1}$.
(d) Show that $D$ has coordinates $(5,4)$.
(e) Find the area of triangle $A C D$.

